# Vapor-Liquid Equilibrium of the $\mathbf{C H}_{\mathbf{4}}-\mathbf{C O}_{\mathbf{2}}$ System at Low Temperatures 

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#### Abstract

This paper reports the bubble-point compositions in the low-temperature region of the methane-carbon dioxide phase dlagram. Liquid compositions in equllibrium with vapor were measured as a function of pressure on isotherms at $-65.00,-81.40,-94.00,-112.00,-130.00$, -148.00 , and $-184.00^{\circ} \mathrm{F}(-53.89,-63.00,-70.00,-80.00$, $-90.00,-100.00$, and $-120.00^{\circ} \mathrm{C}$ ). The smoothed results were combined with prevlous dew-point data to provide tables and plots of isobaric and lsothermal $K$ values. The experimental method used was the vapor-recycle method in a temperature-controlled equillbrium cell with chromatographic analysis of the phases.


## Introduction

Pikaar (7) reported the compositions of the liquid phase in equilibrium with solid $\mathrm{CO}_{2}$ and of the vapor phase in equilibrium with solid $\mathrm{CO}_{2}$ in the solid-liquid and solid-vapor regions, respectively, of the phase diagram for the system methane-carbon dioxide. Hwang et al. (4) reported the compositions of the vapor phase in equilibrium with liquid in the liquid-vapor region of the diagram. In order to complete the phase diagram of this important system, the present work was undertaken to determine the liquid compositions in the same liquid-vapor region as that studied by Hwang et al. For a typical example of the isothermal phase diagrams of the $\mathrm{CH}_{4}-\mathrm{CO}_{2}$ system at low temperatures, see Figure 1, which shows those portions of the diagram which have been determined by the various investigators. Hwang et al. chose to work on isotherms such that many of their temperatures would correspond to those reported in the earlier work of Pikaar. The same strategy has been followed in the present work, in that all of the isotherms reported here (except for that at $-65.00^{\circ} \mathrm{F}$, which is above the triple point of $\mathrm{CO}_{2}$ ) correspond exactly to temperatures studied by both Pikaar and Hwang et al.

A literature review of the previous investigations on this system has been given by Hwang et al. (4).

## Callbration of the Chromatographic System

The method of calibration of the chromatographic system has been described in detail (6). Briefly it consists of preparing a calibration curve of thermal conductivity detector response vs. known compositions of $\mathrm{CH}_{4}-\mathrm{CO}_{2}$ gas mixtures. Individual streams of $\mathrm{CH}_{4}$ and $\mathrm{CO}_{2}$ of known molar flow rates are pumped by two precision positive displacement pumps into a mixing valve. In this manner gas streams ranging in composition from 0.02 to 0.997 mol fraction $\mathrm{CH}_{4}$ are prepared and passed into the chromatographic system for analysis. The resulting calibration curve is then used to determine the compositions of mixtures withdrawn from the equilibrium cell during the lowtemperature measurements.

## Experimental Apparatus and Procedure

For the present measurements, a new vapor-liquid equilibrium cryostat was constructed in the Chemical Engineering Machine Shop at Rice University. This apparatus is essentially an improved version of similar cryostats described previously (1). $\mathrm{CO}_{2}$ and $\mathrm{CH}_{4}$ are introduced into a stainless steel equilibrium cell held
at low temperatures in a bath of isohexane, which is then further cooled to the desired temperature. The bath is under a cooling load produced by liquid nitrogen circulating through copper coils; in order to maintain the temperature constant at the desired value, the cooling is balanced by heat supplied by a Thermotrol (10) temperature controller, which maintains the temperature constant to generally better than $\pm 0.02{ }^{\circ} \mathrm{F}\left( \pm 0.01^{\circ} \mathrm{C}\right)$. The temperature is determined with a Leeds and Northrup platinum thermometer, mounted in the wall of the equilibrium cell, whose resistance is measured on a Leeds and Northrup Mueller bridge. The galvanometer signal from the bridge is fed to a null detector, whose output in turn is fed to a strip chart recorder. In this way, deviations from the set temperature can be monitored continuously.

The vapor in the cell is recycled through the liquid by means of a magnetic pump ( 8 ) until equilibrium is achieved. Pressure in the cell is measured by means of precision Heise gauges. The equilibrium cell is equipped with glass windows, and the bath Dewar is windowed, so the phases can be visually observed in the cell.

After equilibrium is reached, the sample line to the chromatograph is evacuated, and a valve mounted on the cell is opened to withdraw sample into the line. There are valves located at the top, middle, and bottom of the cell, so that either a liquid or a vapor sample can be taken. The parts of the sample lines which pass through the bath fluid are heated to ensure immediate vaporization of the sample. Before entering the chromatographic oven, the sample streams enter a stainless steel mixing vessel, consisting of a Teflon-coated stirring bar which, when magnetically driven, agitates a number of glass beads against the walls and lid of the vessel. The emerging gas stream is thus ensured of complete homogeneity. This stream is then taken into the chromatographic unit and analyzed, using the calibration curve to determine the composition of the unknown sample from its detector response.

A twin $250-\mathrm{cm}^{3}$ capacity positive displacement pump is connected to the equilibrium cell to provide a means of adjusting the pressure in the cell. When very low temperatures are desired, the equilibrium cell is cooled with only pure $\mathrm{CH}_{4}$ present in order to prevent the formation of solid $\mathrm{CO}_{2}$ upon cooling. With the valve to the cell closed, a mixture is prepared in the $500-\mathrm{cm}^{3}$ pump at room temperature at approximately the right composition to give only liquid and vapor phases at the low temperature of the cell. To ensure homogeneity, this mixture is cycled back and forth between the twin $250-\mathrm{cm}^{3}$ cylinders of the $500-\mathrm{cm}^{3}$ pump. When the mixture is let into the cell, a liquid phase invariably condenses without the danger of solid $\mathrm{CO}_{2}$ formation.

## Materials

The methane used in this research was Matheson purity $\mathrm{CH}_{4}$ (minimum purity $99.99 \%$ ), and the carbon dioxide used was Coleman Instrument Grade $\mathrm{CO}_{2}$ (minimum purity $99.99 \%$ ), both from Matheson Gas Products. All materials were used as received without further purification.

## Experimental Results

To check the performance of the new apparatus against previous, well-established equipment, vapor compositions were


Figure 1. Schematic phase diagram for the methane-carbon dioxide system at low temperature.

Table I. Comparison of Present Data with Previous Work ${ }^{a}$

|  |  | Mole fraction $\mathrm{CO}_{2}$ in vapor phase |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $t,{ }^{\circ} \mathrm{F}$ | $P$, psia | Hwang <br> et al. | This <br> work | Difference | \% <br> differ- <br> ence |
| -65.0 | 700 | 0.205 | 0.1922 | 0.0128 | 6.2 |
|  | 800 | 0.2003 | 0.1885 | 0.0118 | 5.9 |
|  | 900 | 0.211 | 0.1973 | 0.0137 | 6.5 |
| -81.4 | 800 | 0.148 | 0.1412 | 0.0068 | 4.6 |
| -94.0 | 750 | 0.1054 | 0.1025 | 0.0029 | 2.8 |
|  | 770 | 0.110 | 0.1064 | 0.0036 | 3.3 |
| -112.0 | 625 | 0.0512 | 0.0510 | 0.0002 | 0.4 |
|  | 640 | 0.0446 | 0.0457 | -0.0011 | -2.5 |
|  | 650 | 0.0409 | 0.0418 | -0.0009 | -2.2 |
|  | 670 | 0.0323 | 0.0331 | -0.0008 | -2.5 |

## ${ }^{a}$ Reference 4.

measured at several temperatures and compared to those measured by the elution method of Hwang et al. (4). When plotted vs. pressure at a given temperature, the present data at the higher temperatures fell on a curve parallel to the previous work but displaced in composition. Typical data are shown in Table I.

It was originally thought that each apparatus had an approximate error of about $1 \%$ in the ability to determine the mole fraction of carbon dioxide in a given mixture. Several factors that might have been able to produce the larger discrepancies of Table I were carefully investigated, but no satisfactory answer was discovered. It seems probable, therefore, that the original estimates of a $1 \%$ accuracy in calibration combined with low-temperature sampling may have been too optimistic for both methods, and perhaps a $\pm 2 \%$ total error would be more realistic for each method.

It should be pointed out, however, that the difference between the present work and that of Hwang et al. is still not a tremendous amount, and the difference gradually decreases with decreasing $\mathrm{CO}_{2}$ concentration until, at $-112^{\circ} \mathrm{F}$, there is no real discrepancy, even on a percentage basis, outside of experimental error. No comparisons between the two apparati were made at temperatures lower than $-112^{\circ} \mathrm{F}$. However, as can be seen from Figure 3, the excellent extrapolation of the liq-uid-phase data to the accurately known vapor pressure of pure $\mathrm{CH}_{4}$ would seem to preclude any chance of a serious error at the temperatures -130 and $-148^{\circ} \mathrm{F}$.

All the experimental data are shown in Table II and Figures 2 and 3 , which are largely self-explanatory. Note that there is an inflection point in each of the liquidus curves for temperatures above the critical point of methane. It should also be pointed out that the data at $-184^{\circ} \mathrm{F}$ were taken under rather severe conditions. Since the calibration curve for sample analysis only


Figure 2. Pressure-composition dlagram for the methane-carbon dioxide system for temperatures above critical temperature of methane: $O$, this work; $\square$, Hwang et al. (4); $\Delta$, vapor pressure of $\mathrm{CO}_{2}$ from ref 9.


Flgure 3. Pressure-composition diagram for the methane-carbon dioxide system for temperatures below critical temperature of methane: O, this work; $\square$, Hwang et al. (4); $\Delta$, vapor pressure of methane from ref 11 and 12. The dotted lines at -130 and $-148^{\circ} \mathrm{C}$ represent the vapor lines "normalized" for slight Heise gauge discrepancies. The pressures in parentheses at $-184^{\circ} \mathrm{F}$ represent pressures when the lines are "normalized" to the known vapor pressure of methane, 171.0 psia, from ref 11 and 12.
extended to 0.997 mol fraction methane $\left(0.003 \mathrm{CO}_{2}\right)$, three of the compositions reported at $-184^{\circ} \mathrm{F}$ are beyond the range of calibration, and the fourth is on the very end of it.

To arrive at these approximate values for composition, the calibration data were extrapolated. Therefore, the points at -184 ${ }^{\circ} \mathrm{F}$ must carry more than the usual uncertainty in composition. Furthermore, it will be seen that all the pressures reported at $-184^{\circ} \mathrm{F}$ are actually above the accepted vapor pressure of pure $\mathrm{CH}_{4}$ (171.0 psia) $(11,12)$. This is especially surprising since the results at -130 and $-148^{\circ} \mathrm{F}$ extrapolate perfectly to the correct vapor pressure of $\mathrm{CH}_{4}$ (Figure 3). The discrepancy in pressure at $-184^{\circ} \mathrm{F}$ can only be attributed to the 1000 psia Heise gauge used in the present work, whose stated accuracy is $\pm 1$ psia, but which, it must be assumed, could have been off in this case by about 2.5 psia. Despite all these complications, it still appears that the data at $-184^{\circ} \mathrm{F}$ are of some value, since the pressures can be corrected to the true pressures, and all four compositions at this temperature were taken from the extrapolated calibration curve described above. Therefore there should be a good measure of relative consistency among them,

Table II. Experimental Vapor-Liquid Equilibrium Data for the Methane-Carbon Dioxide System

| Pressure, psia | Mole Fraction of $\mathrm{CO}_{2}$ | Pressure, psia | Mole Fraction of $\mathrm{CO}_{2}$ |
| :---: | :---: | :---: | :---: |
| $t=-65.00^{\circ} \mathrm{F}=-53.89{ }^{\circ} \mathrm{C} \quad t=-81.40{ }^{\circ} \mathrm{F}=-63.00^{\circ} \mathrm{C}$ |  |  |  |
| Liquid |  | Liquid |  |
| $84.4{ }^{\text {a }}$ | 1.0000 | 625.0 | 0.6825 |
| 396.0 | 0.8965 | 675.0 | 0.5944 |
| 495.1 | 0.8493 | 725.0 | 0.4795 |
| 601.7 | 0.7811 | 776.4 | 0.3478 |
| 698.0 | 0.6972 | 809.7 | 0.2761 |
| 757.0 | 0.6265 | 839.4 | 0.2152 |
| 807.9 | 0.5512 | Vapor |  |
| 852.2 | 0.4735 |  |  |
| 880.7 | 0.4175 | 199.0 | 0.1412 |
| 909.2 | 0.3606 | Critical |  |
| 925.1 | 0.3242 | 845.5 |  |
| 932.8 | 0.3061 |  | $t=-94.00^{\circ} \mathrm{F}=-70.00^{\circ} \mathrm{C}$ |  |
| 935.9 | 0.2969 |  |  |  |
| Vapor |  | Liquid |  |
| $84.4{ }^{\text {a }}$ | 1.0000 | 710.1 | 0.2509 |
| 125.6 | 0.6889 | 720.0 | 0.2317 |
| 147.9 | 0.5951 | 730.0 | 0.2121 |
| 186.1 | 0.4859 | 740.0 | 0.1949 |
| 225.2 | 0.4131 | 750.0 | 0.1771 |
| 297.9 | 0.3280 | 760.3 | 0.1593 |
| 399.8 | 0.2620 | 770.3 | 0.1407 |
| 515.7 | 0.2222 | Vapor |  |
| 615.7 | 0.2021 | 750.0 | 0.1025 |
| 717.8 | 0.1911 | 770.2 | 0.1064 |
| 805.8 | 0.1884 | Critical |  |
| 870.9 | 0.1925 |  |  |  |  |
| 919.9 | 0.2046 | 775.2 | 0.1216 |
| Critical |  | $t=-148.00^{\circ} \mathrm{F}=-100.00^{\circ} \mathrm{C}$ |  |
| 940.8 | 0.2517 | Liquid |  |
| $t=-112.00^{\circ} \mathrm{F}=-80.00^{\circ}$ |  | 362.3 | 0.0370 |
|  |  | 366.4 | 0.0270 |
| Liquid |  | 370.4 | 0.0172 |
| 625.0 | 0.1083 | 374.0 | 0.0083 |
| 640.0 | 0.0864 | $377.8^{\text {b }}$ | 0.0000 |
| 655.0 | 0.0672 | $\begin{aligned} t= & -184.00^{\circ} \mathrm{F}= \\ & -120.00^{\circ} \mathrm{C}^{\mathrm{c}} \end{aligned}$ |  |
| 670.0 | 0.0491 |  |  |  |  |
| 680.0 | 0.0378 |  |  |  |  |
| 685.0 | 0.0326 | Liquid |  |
| Vapor |  | 172.4 | 0.0059 |
| 625.0 | 0.0510 | 173.3 | 0.00105 |
| 639.9 | 0.0457 | Vapor |  |
| 650.0 | 0.0418 | 172.4 | 0.00099 |
| 670.0 | 0.0331 | 173.3 | 0.00016 |
| Critical |  |  |  |
| 687.5 |  |  |  |
| $t=-130.00^{\circ} \mathrm{F}=-90.0{ }^{\circ} \mathrm{C}$ |  |  |  |
| Liquid |  |  |  |
| 494.2 | 0.0547 |  |  |
| 500.0 | 0.0451 |  |  |
| 504.9 | 0.0370 |  |  |
| 513.0 | 0.0238 |  |  |
| 520.0 | 0.0130 |  |  |
| 524.9 | 0.0058 |  |  |
| $528{ }^{\text {b }}$ | 0.0000 |  |  |

${ }^{a}$ Vapor pressure of pure $\mathrm{CO}_{2}$ from ref 9 . ${ }^{b}$ Vapor pressure of pure $\mathrm{CH}_{4}$ from ref 11,12 . ${ }^{c}$ For explanation of how this isotherm was treated, see text.
and the $K$ values taken from them should be of value.

## Smoothed Data and K Values

The data of Table II were combined with those reported for the dew-point compositions by Hwang et al. (4) to provide smoothed values for the vapor-liquid equilibria of the meth-


Flgure 4. Isothermal $K$ values for the methane-carbon dioxide system.
ane-carbon dioxide system. Because of the slight discrepancies between the two sets of data, certain judgments were made in order to treat the data such that the two sets would be "normalized" against each other. In this fashion each set was recognized to have high internal precision and was therefore adjusted slightly at each temperature in order to match the other at some common point. Thus the $K$ values would be expected to be much better than those that could be calculated from the two separate sets of raw data.

At $-65^{\circ} \mathrm{F}$, the experimental data from this work were smoothed to give liquid and vapor compositions at even pressures. At -81.4 and $-94.0^{\circ} \mathrm{F}$, the shapes of the dew-point curves from the previous study (4) were used but were displaced by a small amount to land on the one or two dew-point data from this work. At $-112.0^{\circ} \mathrm{F}$, since the discrepancies between the two sets of data (see Table I) are within the experimental error, the dew-point data from previous work (4) were combined with the bubble-point data to provide the $K$ values.

For the three lowest temperatures ( $-130.0,-148.0$, and $-184.0^{\circ} \mathrm{F}$ ), the experimental results indicate that the pres-sure-composition curves, i.e., isothermal $P-x$ and $P-y$ curves, are linear. In this case, the $K$ values can be calculated from the vapor pressure of methane and the slopes of both $P-x$ and $P-y$ curves (see Appendix).

The smoothed vapor-liquid equilibrium data are shown in Table III. Note the constancy of the $K$ values for carbon dioxide for each of the three lowest temperatures.

Figure 4 presents the data in the form of $K$ values vs. pressure. Figure 5 and Table IV show the smoothed (from K-P

Table III. Smoothed Vapor-Liquid Equilibrium Data of Methane-Carbon Dioxide System

| $P$, psia | $P$, atm | ${ }^{\mathrm{CH}_{4}}$ | $y_{\mathrm{CH}_{4}}$ | $K_{\mathrm{CH}_{4}}$ | $K_{\mathrm{CO}_{2}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $t=-65.00{ }^{\circ} \mathrm{F}=-53.89{ }^{\circ} \mathrm{C}$ |  |  |  |  |  |
| $84.4{ }^{\text {a }}$ | 5.74 | 0.0 | 0.0 | $46.40^{\text {b }}$ | 1.00 |
| 100 | 6.80 | 0.0049 | 0.1860 | 37.96 | 0.8180 |
| 200 | 13.61 | 0.0355 | 0.5461 | 15.38 | 0.4706 |
| 300 | 20.41 | 0.0681 | 0.6745 | 9.905 | 0.3493 |
| 400 | 27.22 | 0.1054 | 0.7384 | 7.006 | 0.2924 |
| 500 | 34.02 | 0.1535 | 0.7740 | 5.042 | 0.2670 |
| 600 | 40.83 | 0.2180 | 0.7960 | 3.651 | 0.2609 |
| 700 | 47.63 | 0.3056 | 0.8078 | 2.643 | 0.2768 |
| 800 | 54.44 | 0.4368 | 0.8115 | 1.858 | 0.3347 |
| 900 | 61.24 | 0.6204 | 0.8027 | 1.294 | 0.5198 |
| 920 | 62.60 | 0.6620 | 0.7948 | 1.201 | 0.6071 |
| $939^{c}$ | 63.83 | 0.7483 | 0.7483 | 1.000 | 1.0000 |
| $t=-81.40{ }^{\circ} \mathrm{F}=-63.00^{\circ} \mathrm{C}$ |  |  |  |  |  |
| $612^{\text {d }}$ | 41.64 | 0.3062 | 0.8482 | $2.770^{e}$ | $0.2188^{f}$ |
| 625 | 42.53 | 0.3175 | 0.8568 | 2.699 | 0.2098 |
| 650 | 44.23 | 0.3604 | 0.8587 | 2.383 | 0.2209 |
| 675 | 45.93 | 0.4056 | 0.8596 | 2.119 | 0.2362 |
| 700 | 47.63 | 0.4555 | 0.8602 | 1.888 | 0.2567 |
| 725 | 49.33 | 0.5205 | 0.8609 | 1.654 | 0.2901 |
| 750 | 51.03 | 0.5881 | 0.8610 | 1.464 | 0.3375 |
| 775 | 52.74 | 0.6486 | 0.8608 | 1.327 | 0.3961 |
| 800 | 54.44 | 0.7018 | 0.8587 | 1.224 | 0.4738 |
| 825 | 56.14 | 0.7544 | 0.8539 | 1.132 | 0.5949 |
| $845^{\text {c }}$ | 57.50 | 0.8370 | 0.8370 | 1.000 | 1.0000 |
| $t=-94.00^{\circ} \mathrm{F}=-70.00^{\circ} \mathrm{C}$ |  |  |  |  |  |
| $700^{\text {d }}$ | 47.63 | 0.7307 | 0.8914 | $1.220^{e}$ | $0.4033{ }^{f}$ |
| 710 | 48.31 | 0.7491 | 0.8952 | 1.195 | 0.4177 |
| 720 | 48.99 | 0.7683 | 0.8962 | 1.166 | 0.4480 |
| 730 | 49.67 | 0.7879 | 0.8973 | 1.139 | 0.4842 |
| 740 | 50.35 | 0.8051 | 0.8976 | 1.115 | 0.5254 |
| 750 | 51.03 | 0.8229 | 0.8978 | 1.091 | 0.5771 |
| 760 | 51.71 | 0.8388 | 0.8967 | 1.069 | 0.6408 |
| 770 | 52.40 | 0.8568 | 0.8933 | 1.043 | 0.7451 |
| $774{ }^{\text {c }}$ | 52.67 | 0.8784 | 0.8784 | 1.000 | 1.0000 |
| $t=-112.00^{\circ} \mathrm{F}=-80.00^{\circ} \mathrm{C}$ |  |  |  |  |  |
| $622^{\text {d }}$ | 42.32 | 0.8853 | 0.9473 | $1.0700^{e}$ | $0.4595{ }^{\prime}$ |
| 630 | 42.87 | 0.8992 | 0.9507 | 1.0573 | 0.4891 |
| 640 | 43.55 | 0.9136 | 0.9554 | 1.0457 | 0.5162 |
| 650 | 44.23 | 0.9272 | 0.9591 | 1.0344 | 0.5618 |
| 660 | 44.91 | 0.9385 | 0.9635 | 1.0266 | 0.5935 |
| 670 | 45.59 | 0.9517 | 0.9677 | 1.0168 | 0.6687 |
| 680 | 46.27 | 0.9622 | 0.9718 | 1.0100 | 0.7460 |
| $687^{c}$ | 46.75 | 0.9736 | 0.9736 | 1.0000 | 1.0000 |
| $t=-130.00^{\circ} \mathrm{F}=-90.00^{\circ} \mathrm{C}^{g}$ |  |  |  |  |  |
| $487.3^{\text {d }}$ | 33.16 | 0.9350 | 0.9770 | $1.0449^{e}$ | $0.3540^{f}$ |
| 490.0 | 33.34 | 0.9393 | 0.9785 | 1.0418 | 0.3540 |
| 500.0 | 34.02 | 0.9553 | 0.9842 | 1.0303 | 0.3540 |
| 510.0 | 34.70 | 0.9712 | 0.9898 | 1.0191 | 0.3540 |
| 520.0 | 35.38 | 0.9872 | 0.99547 | 1.0084 | 0.3540 |
| $528.0^{h}$ | 35.93 | 1.000 | 1.000 | 1.0000 | $0.3540^{i}$ |
| $t=-148.00^{\circ} \mathrm{F}=-100.00^{\circ} \mathrm{C}^{\text {g }}$ |  |  |  |  |  |
| $357.7^{\text {d }}$ | 24.34 | 0.9507 | 0.9896 | $1.0409^{e}$ | $0.2112^{f}$ |
| 360 | 24.50 | 0.9563 | 0.99078 | 1.0360 | 0.2112 |
| 365 | 24.84 | 0.9686 | 0.99337 | 1.0256 | 0.2112 |
| 370 | 25.18 | 0.9809 | 0.99596 | 1.0154 | 0.2112 |
| $377.8^{h}$ | 25.71 | 1.0000 | 1.0000 | 1.0000 | $0.2112^{\text {i }}$ |
| 169.5 $\quad t=-184.00^{\circ} \mathrm{F}=-120.00^{\circ} \mathrm{C}^{g}$ |  |  |  |  |  |
| $169.5^{\text {d }}$ | 11.53 | 0.99192 | 0.99859 | $1.0067{ }^{\text {e }}$ | $0.1751{ }^{f}$ |
| 170.0 | 11.57 | 0.99461 | 0.999057 | 1.0045 | 0.1751 |
| 170.5 | 11.60 | 0.99730 | 0.999528 | 1.0022 | 0.1751 , |
| $171.0^{h}$ | 11.64 | 1.0000 | 1.0000 | 1.0000 | $0.1751^{i}$ |

${ }^{a}$ Vapor pressure of carbon dioxide from ref $9 .{ }^{b} K_{\mathrm{CH}_{4}}{ }^{\infty}$.
${ }^{c}$ Critical point of mixture, ${ }^{d}$ Triple-point pressure mixture from ref 2 and 3. ${ }^{e} K_{\mathrm{CH}_{4}}$ SLV. $f^{\prime} \mathrm{CO}_{2}{ }^{\text {SLV }}$. s See Appendix for explanation of how these isotherms were treated. $h$ Vapor pressure of methane from ref 11 and $12 .{ }^{i} K_{\mathrm{CO}_{2}}{ }^{\infty}$.
plot) isobaric $K$ values in the high-temperature region


Flgure 5. Isobaric $K$ values for the methane-carbon dioxide system.
Table IV. Smoothed Isobaric $K$ Values for Methane-Carbon Dioxide System

| $P$, psia | ,${ }^{\circ} \mathrm{F}$ | $K_{\mathrm{CO}_{2}}$ | $K_{\mathrm{CH}_{4}}$ |
| :---: | :--- | :--- | :--- |
| 150 | $-38.6^{a}$ | 1.0 | $25.5^{b}$ |
|  | -40.0 | 0.974 | 25.3 |
|  | -65.0 | 0.587 | 22.6 |
|  | $-69.88^{c}$ | 0.515 | 21.8 |
|  | $-71.5^{d}$ | $0.500^{e}$ | $21.4^{f}$ |
|  | $-23.6^{a}$ | 1.0 | $18.9^{b}$ |
|  | -40.0 | 0.782 | 18.0 |
|  | -65.0 | 0.464 | 15.8 |
|  | $-69.88^{c}$ | 0.409 | 14.9 |
| 300 | $-72.5^{d}$ | $0.370^{e}$ | $14.6^{f}$ |
|  | $-0.9^{a}$ | 1.0 | $12.1^{b}$ |
|  | -4.0 | 0.960 | 12.0 |
|  | -40.0 | 0.583 | 10.8 |
|  | -65.0 | 0.343 | 9.60 |
|  | $-69.88^{c}$ | 0.295 | 9.40 |
|  | $-74.5^{d}$ | $0.248^{e}$ | $9.10^{f}$ |
|  | $16.5^{a}$ | 1.0 | $8.80^{b}$ |
|  | -4.0 | 0.800 | 8.39 |
|  | -40.0 | 0.480 | 7.50 |
|  | -65.0 | 0.289 | 6.57 |
|  | $-69.88^{c}$ | 0.251 | 6.34 |
|  | $-76.5^{d}$ | $0.200^{e}$ | $6.00^{f}$ |
| 500 | $31.4^{a}$ | 1.0 | $6.80^{b}$ |
|  | -4.0 | 0.702 | 6.27 |
|  | -40.0 | 0.418 | 5.50 |
|  | -65.0 | 0.263 | 4.77 |
|  | $-69.88^{c}$ | 0.239 | 4.56 |
|  | $-79.0^{d}$ | $0.197^{e}$ | $4.11^{f}$ |

${ }^{a}$ Saturation temperature of carbon dioxide from ref 9.
${ }^{b} \mathrm{~K}_{\mathrm{CH}_{4}}{ }^{\infty}$. ${ }^{c}$ Triple-point temperature of carbon dioxide from ref $9 .{ }^{4}{ }^{d}$ Triple-point temperature of mixture from ref 2 and 3.
${ }^{e} \mathrm{~K}_{\mathrm{CO}_{2}} \mathrm{SLV} .{ }_{f} \mathrm{~K}_{\mathrm{CH}_{4}} \mathrm{SLV}$.

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Appendix. K Values for the Methane-Carbon Dioxide System at Low Temperatures

The linear relationships between the system pressure and compositions can be expressed as
$P=m^{\mathrm{L}} x_{\mathrm{CO}_{2}}+b^{\mathrm{L}}$
and
$P=m^{\mathrm{V}} y_{\mathrm{CO}_{2}}+b^{\mathrm{V}}$
where $P=$ system pressure, $x_{\mathrm{CO}_{2}}=$ mole fraction of $\mathrm{CO}_{2}$ in the liquid phase, $y_{\mathrm{CO}_{2}}=$ mole fraction of $\mathrm{CO}_{2}$ in the vapor phase, $m^{\mathrm{L}}, m^{\vee}=$ slopes of the $P-x_{\mathrm{CO}_{2}}$ and $P-y_{\mathrm{CO}_{2}}$ curves, respectively, and $b^{\llcorner }, b^{\vee}=$ intercepts of eq 1 and 2 at $x_{\mathrm{CO}_{2}}=y_{\mathrm{CO}_{2}}=0$.

When $x_{\mathrm{CO}_{2}}=y_{\mathrm{CO}_{2}}=0$, the system pressure will be equal to the vapor pressure of pure methane $\left(P^{*}{ }_{\mathrm{CH}}^{4}\right.$ ) $)$ at system temperature. Thus
$b^{\mathrm{L}}=b^{\mathrm{V}}=P^{*} \mathrm{CH}_{4}$
Therefore, eq 1 and 2 become
$P=m^{\mathrm{L}} x_{\mathrm{CO}_{2}}+P{ }^{*} \mathrm{CH}_{4}$
$P=m^{\mathrm{v}} y_{\mathrm{CO}_{2}}+P^{*} \mathrm{CH}_{4}$
then

$$
\begin{aligned}
K_{\mathrm{CO}_{2}} & \equiv y_{\mathrm{CO}_{2}} / x_{\mathrm{CO}_{2}} \\
& =\frac{\left(P-P{ }^{*} \mathrm{CH}_{4}\right) / m^{\mathrm{V}}}{\left(P-P{ }_{\mathrm{CH}_{4}}\right) / m^{\mathrm{L}}} \\
& =\frac{m^{\mathrm{L}}}{m^{\mathrm{V}}} \\
& =\frac{\text { slope of } P-x_{\mathrm{CO}_{2}} \text { curve }}{\text { slope of } P-y_{\mathrm{CO}_{2}} \text { curve }} \\
& =\text { function of system temperature only }
\end{aligned}
$$

and

$$
\begin{aligned}
K_{\mathrm{CH}_{4}} & \equiv y_{\mathrm{CH}_{4}} / x_{\mathrm{CH}_{4}} \\
& =\left(1-y_{\mathrm{CO}_{2}}\right) /\left(1-x_{\mathrm{CO}_{2}}\right) \\
& =\frac{m^{\mathrm{L}}\left(m^{\mathrm{V}}-P+P^{*}{ }_{\mathrm{CH}_{4}}\right)}{m^{\mathrm{V}}\left(m^{\mathrm{L}}-P+P^{*}{ }_{\mathrm{CH}_{4}}\right)}
\end{aligned}
$$

$=$ function of system temperature and pressure
A least-squares linear regression method was used to fit the experimental $P-x_{\mathrm{CO}_{2}}$ and $P-y_{\mathrm{CO}_{2}}$ data and obtain the slopes for each isotherm. Results are as follows:

| $T,{ }^{\circ} \mathrm{F}$ | $10^{-3} m^{\mathrm{L}}$ | $10^{-4} m^{\mathrm{V}}$ | $K_{\mathrm{CO}_{2}}=m^{\mathrm{L}} / m^{\mathrm{V}}$ |
| :---: | :---: | :---: | :---: |
| -130.00 | -0.62571 | -0.17677 | 0.3540 |
| -148.00 | -0.40769 | -0.19302 | 0.2112 |
| -184.00 | -0.18557 | -0.10600 | 0.1751 |

The smoothed vapor-liquid equilibrium data can be calculated from the following equations at different system pressures:

$$
\begin{align*}
& x_{\mathrm{CO}_{2}}=\left(P-P^{*}{ }_{\mathrm{CH}_{4}}\right) / m^{\mathrm{L}}  \tag{5}\\
& y_{\mathrm{CO}_{2}}=\left(P-P^{*} \mathrm{CH}_{4}\right) / m^{\mathrm{V}} \tag{6}
\end{align*}
$$

and
$K_{\mathrm{CH}_{4}}=\left(1-y_{\mathrm{CO}_{2}}\right) /\left(1-x_{\mathrm{CO}_{2}}\right)$

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# On the Solubility of Benzoic Acid in Aqueous Carboxymethylcellulose Solutions 

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## Solubility of benzoic acid in distilled and demineralized

 water and aqueous CMC solutions containing $0.5,1.0,1.5$, and $\mathbf{2 . 0 \%}$ polymer by weight has been determined in the temperature range of $15-45{ }^{\circ} \mathrm{C}$. At any given temperature, the solubility in the polymer solution Increases with polymer concentration and seems to approach a constant value at higher concentrations.
## Introduction

Dissolution rate studies of low-solubility organic compounds such as benzoic acid, 2-naphthol, etc., have been frequently used as a technique in mass transfer investigations with Newtonian fluids. Such solutes have many inherent advantages. They can be easily molded and pelletized into various shapes. Their solubilities are of moderate range and the analytical procedures are simple. Above all, the dissolution of these

